projection of the $\mathrm{C}(5) \mathrm{C}(6) \mathrm{C}(7)$-moiety (the ' t -Bu' group) along the $\mathrm{C}(4) \mathrm{C}(3)$ bond is given in Fig. 2(b). An average twist from the perfectly staggered position of $17.4^{\circ}$ is observed.
The molecular strain is relieved by an overall flattening of the chair and not by adopting a 'twist' conformation. The distortion of the ring and the observed twist of the ' t -Bu' group may be due to nonbonded contacts between the methyl-hydrogen atoms and ring-hydrogen atoms. Relevant contacts, smaller than $2.50 \AA$, are shown in Fig. 4. As far as we know this is the first 1,2 -diaxially substituted cyclohexane chair thus far reported.
The $\mathrm{C}(4) \mathrm{C}(7) \mathrm{O}(1) \mathrm{O}(2)$-group is planar within experimental error. The atoms $C(5)$ and $C(8)$ are 0.155 and $0 \cdot 128 \AA$ at either side from this plane. The $\mathrm{C}=\mathrm{O}$ and $\mathrm{C}(4)-\mathrm{C}(5)$ bonds deviate $6.2^{\circ}$ from being eclipsed [Fig. 2(c)]. This orientation is in excellent agreement with the situation usually found in aliphatic carboxylic acids (Kanters, Kroon, Peerdeman \& Schoone, 1967) and with the conformation of an axial carboxyl group in cyclohexanecarboxylic acids (van Koningsveld, 1972 and references cited therein). The orientation of the methyl groups is shown in Fig. 3. The large $\mathbf{H}(82) \mathbf{C}(8) \mathbf{H}(83)$ angle ( $136^{\circ}$ ) cannot be conclusively explained.
The packing of the molecules in the crystal is illustrated in Fig. 4. The cyclohexane rings form strings along the [110] direction. The strings are held together by non-bonding contacts between the 2 -carboxy-methyl-2-propyl groups. Some short hydrogen-hydrogen distances $(<2 \cdot 50 \AA)$ are given in the figure.

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# An X-ray Study of Two Phases of $\mathrm{BaFeO}_{3-\boldsymbol{x}}$ 

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$\mathrm{BaFeO}_{3-x}$ shows several phases depending upon the iron valence. In $\alpha-\mathrm{BaFeO}_{2.5}$, which is orthorhombic, with $a=5.911 \pm 0.003, b=16.450 \pm 0.008, c=11.037 \pm 0.006 \AA$, the iron atom is strictly trivalent. $\mathrm{BaFeO}_{2 \cdot 67}$, which is hexagonal with $a=5.683 \pm 0.002, c=13.916 \pm 0.005 \AA$, space group $P 6_{3} / m m c$, is isomorphous with $\mathrm{BaTiO}_{3}$.

## Introduction

The compound $\mathrm{BaFeO}_{3-x}$, barium orthoferrate, has been examined by many authors (Erchak, Fankuchen \& Ward, 1946; Malinofsky \& Kedesdy, 1954; Brisi, 1955; Gallagher, MacChesney \& Buchanan, 1965; MacChesney, Potter, Sherwood \& Williams, 1965; Mori, 1966) to determine its phase equilibrium diagram and structural properties.

The valence of the iron atom and the crystal structure of barium orthoferrate depend upon temperature, firing atmosphere and cooling rate.

The present investigation was undertaken to ascertain the isomorphism between hexagonal $\mathrm{BaFeO}_{3-x}$ and $\mathrm{BaTiO}_{3}$, suggested by Malinofsky \& Kedesdy (1954), Brisi (1955), Gallagher et al. (1965), MacChesney et al. (1965), and Mori (1966) and to determine the crystal data of a phase quenched at
temperatures higher than $915^{\circ} \mathrm{C}$ and hereafter called $\alpha-\mathrm{BaFeO}_{2.5}$, with the iron atom strictly trivalent.

## Experimental

The $\alpha-\mathrm{BaFeO}_{2.5}$ phase was obtained by sintering pressed pellet mixtures of $\mathrm{BaCO}_{3}$ and $\mathrm{Fe}_{2} \mathrm{O}_{3}$ in a 2:1 molecular ratio in air at $1300^{\circ} \mathrm{C}$. The sintered product was quenched in air from $1300^{\circ} \mathrm{C}$. Other samples were quenched from $950^{\circ} \mathrm{C}$ and from $1100^{\circ} \mathrm{C}$ respectively. Iodometric analysis of these samples showed that the percentage of $\mathrm{Fe}^{4+}$ was lower than $1 \%$.

Fragments of the compound quenched from $950^{\circ} \mathrm{C}$ were reheated in vacuum at $1100^{\circ} \mathrm{C}$ for several hours and then quenched in vacuum. These fragments did not reveal the presence of $\mathrm{Fe}^{4+}$ on iodometric analysis. The reflexions from these samples were obtained with a Siemens diffractometer and a Guinier camera, using Co $K \alpha$ radiation. All the compounds exhibited the same values of interplanar spacings, which were indexed according to an orthorhombic symmetry.

The $\alpha$-phase was then ground and reheated at $900^{\circ} \mathrm{C}$ in air for several hours and slowly cooled. The product obtained exhibited a hexagonal symmetry and a formula $\mathrm{BaFeO}_{2.67}$ on iodometric determination of the percentage of $\mathrm{Fe}^{4+}$. The structure of this phase, isomorphous with $\mathrm{BaTiO}_{3}$, was determined by recording reflexions with a scintillation counter in conjunction with a pulse-height analyser, using Co $K \alpha$ radiation on a Siemens diffractometer.

## X-ray analysis

MacChesney et al. (1965) reported the data of a phase of barium orthoferrate, with trivalent iron, and suggested it to be orthorhombic ( $a=5.83, b=$ $16.38, c=5.54 \AA$ ). However, the values of the spacing calculated with these parameters did not completely reproduce the X-ray pattern of our compound $\alpha-\mathrm{BaFeO}_{2.5}$. Duplication of the $c$ axis permitted us to index all the reflexions of our pattern. The least-squares refined lattice parameters of this $\alpha$-phase are: $a=5.911 \pm 0.003, b=16.450 \pm 0.008, c=11.037 \pm$ $0.006 \AA$ at room temperature $\left(Z=16, D_{\text {obs }}=5.7 \mathrm{~g} \mathrm{~cm}^{-3}\right.$ $D_{\text {calc }}=5.77 \mathrm{~g} \mathrm{~cm}^{-3}$ ). Systematic extinctions occurred for $h 00$ reflexions with $h \neq 2 n$ and $0 k 0$ with $k \neq 2 n$; no extinction was observed for the general reflexions $h k l$. The proposed space group is $P 2_{1} 2_{1} 2$, No. 18 of International Tables for $X$-ray Crystallography (1952). The final data for the observed and calculated interplanar spacings are reported in Table 1.

The lattice dimensions of $\mathrm{BaFeO}_{3-x}$, hexagonal phase, are a function of the percentage of $\mathrm{Fe}^{4+}$ (Mori, 1966). Our product, $\mathrm{BaFeO}_{2.67}$, gave the least-squares refined lattice parameters $a=b=5.683 \pm 0.002, c=$ $13.916 \pm 0.005 \AA \quad\left(Z=6, \quad D_{\text {obs }}=5.9 \mathrm{~g} \mathrm{~cm}^{-3}, \quad D_{\text {calc }}=\right.$ $6.03 \mathrm{~g} \mathrm{~cm}^{-3}$ ). The $\mathrm{BaTiO}_{3}$ structure, hexagonal, space group $P_{3} / m m c$ (No. 194 of International Tables for

Table 1. Debye-Scherrer diagram of $\alpha-\mathrm{BaFeO}_{2.5}$, orthorhombic phase, at $20^{\circ} \mathrm{C}$

| $h k l$ | $d_{\text {obs }}$ | $d_{\text {calc }}$ | $I_{\text {obs }}$ |
| :---: | :---: | :---: | :---: |
| 001 | 11 | 11.037 | $w$ |
| 040 | $4 \cdot 125$ | $4 \cdot 113$ | $w$ |
| 102 | $4 \cdot 041$ | $4 \cdot 035$ | $m$ |
| 003 | $3 \cdot 675$ | $3 \cdot 679$ | $v w$ |
| 042 | $3 \cdot 303$ | $3 \cdot 297$ | $v w$ |
| 113 | $3 \cdot 070$ | $3 \cdot 069$ | $v w$ |
| 123 | $2 \cdot 928$ | 2.920 | $s$ |
| 210 | 2.906 | 2.909 | $s$ |
| 150 | $2 \cdot 876$ | $2 \cdot 879$ | vs |
| 220 | $2 \cdot 786$ | $2 \cdot 782$ | $s$ |
| 221 | $2 \cdot 704$ | $2 \cdot 700$ | $v w$ |
| 061 | $2 \cdot 653$ | $2 \cdot 660$ | vw |
| 230 | $2 \cdot 601$ | $2 \cdot 602$ | $v w$ |
| 152 | $2 \cdot 552$ | $2 \cdot 550$ | vw |
| 034 | $2 \cdot 463$ | $2 \cdot 464$ | $w$ |
| 124 | $2 \cdot 394$ | $2 \cdot 393$ | $m$ |
| 203 | $2 \cdot 303$ | $2 \cdot 304$ | $w$ |
| 134 | $2 \cdot 276$ | $2 \cdot 275$ | $v w$ |
| 170 | $2 \cdot 185$ | $2 \cdot 184$ | $w$ |
| 054 | $2 \cdot 110$ | $2 \cdot 114$ | $v w$ |
| 105 | $2 \cdot 067$ | $2 \cdot 068$ | $m$ |
| 081 | $2 \cdot 021$ | 2.021 | $m$ |
| 214 | 2.003 | $2 \cdot 002$ | $v w$ |
| 073 | 1.982 | 1.980 | $v w$ |
| 135 | 1.935 | 1.935 | $v w$ |
| 234 | 1.900 | 1.893 | $w$ |
| 312 | $1 \cdot 845$ | $1 \cdot 845$ | $w$ |
| 055 | 1.834 | $\left\{\begin{array}{l}1.834 \\ 1.833\end{array}\right.$ | $v w$ |
| 182 | 1.834 | $\{1.833$ |  |
| 091 | $1 \cdot 803$ | $1 \cdot 803$ | $v w$ |
| 205 | 1.772 | 1.769 | vw |
| 303 | 1.739 | 1.738 | vw |
| 235 | 1.684 | 1.683 | $m$ |
| 281 | 1.668 | 1.668 | $w$ |
| 333 | 1.656 | 1.656 | $w$ |
| 093 | $1 \cdot 635$ | 1.637 | $w$ |
| 245 | $1 \cdot 624$ | $\{1.625$ | $w$ |
| 264 | 1.624 | \{1.624 |  |
| 274 | 1.531 | $1 \cdot 531$ | $v w$ |
| 370 | $1 \cdot 510$ | $1 \cdot 510$ | vw |

Intensities: $v s=$ very strong, $s=$ strong, $m=$ medium, $w=$ weak, $v w=$ very weak.

X-ray Crystallography, 1952), was reported by Burbank \& Evans (1948). The structure of $\mathrm{BaTiO}_{3}$ was tested as a model of $\mathrm{BaFeO}_{2.67}$ by means of a computer program (Smith, 1967). The final agreement index $R=\sum| | I_{o}\left|-\left|I_{c}\right|\right| / \sum\left|I_{o}\right|$ is 0.095 . The structure of $\mathrm{BaFeO}_{2.67}$ is therefore considered to be of the same type as that of $\mathrm{BaTiO}_{3}$.

In terms of the positions of the space group $P 6_{3} / m m c$ the proposed atomic positions are:

$$
\begin{array}{rlll}
2 \mathrm{Ba}(1) \text { in }(b): & 0 & 0 & \frac{1}{4} \\
4 \mathrm{Ba}(2) \text { in }(f): & \frac{1}{3} & \frac{2}{3} & z, z=0.097 \\
2 \mathrm{Fe}(1) \text { in }(a): & 0 & 0 & 0 \\
4 \mathrm{Fe}(2) \text { in }(f): & \frac{1}{3} & \frac{2}{3} & z, z=0.845 \\
* 6 \mathrm{O}(1) \text { in }(h): & x & 2 x & \frac{1}{4}, x=0.522 \\
{ }^{*} 12 \mathrm{O}(2) \text { in }(k): & x & 2 x & z, x=0.836,
\end{array}
$$

Table 2. Debye-Scherrer diagram of $\mathrm{BaFeO}_{2.67}$, hexagonal phase, at $20^{\circ} \mathrm{C}$

| hkl | $d_{\text {obs }}$ | $d_{\text {calc }}$ | $I_{\text {obs }}$ | $I_{\text {catc }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 002 |  | 6.958 | <1 | <1 |
| 101 | 4.635 | $4 \cdot 640$ | 3 | 2 |
| 102 | 4.023 | 4.018 | 15 | 10 |
| 004 |  | $3 \cdot 479$ | <1 | 1 |
| 103 | 3.378 | $3 \cdot 376$ | 33 | 40 |
| 110 | $2 \cdot 841$ | $\{2.842$ | 170 | $\{100$ |
| 104 | 2.841 | $\{2.841$ | 170 | \{ 70 |
| 112 |  | 2.631 | <1 | <1 |
| 201 | $2 \cdot 420$ | $\{2.423$ | 5 | 3 |
| 105 | 2.420 | 2.422 | 5 | 4 |
| 202 |  | $\left\{\begin{array}{l}2.320 \\ 2.319\end{array}\right.$ |  | 10 |
| 006 | 2.319 | $\{2.319$ | 21 |  |
| 114 | $2 \cdot 199$ | $2 \cdot 201$ | 2 | 3 |
| 203 | $2 \cdot 175$ | $2 \cdot 174$ | 23 | 22 |
| 204 | 2.007 | 2.009 | 36 | 33 |
| 211 |  | 1.844 | <1 | 1 |
| 205 | 1.843 | $\{1.8435$ | 13 | 4 |
| 107 | 1.843 | \{ 1.843 | 13 | 11 |
| 212 | 1.798 | $\{1.797$ | 11 | 3 |
| 116 | 1.798 | $\{1.796$ | 11 | 6 |
| 008 |  | 1.739 | <1 | 1 |
| 213 | 1.727 | 1.727 | 7 | 9 |
| 300 |  | \{ 1.641 |  | 17 |
| 214 | $1 \cdot 641$ | 1.6404 | 43 | 24 |
| 108 |  | 1.640 |  | 2 |
| 215 | 1.548 | $\{1.547$ | 8 | 2 |
| 207 | 1.548 | \{ 1.546 | 8 | 7 |
| 118 | 1.485 | 1.487 | 12 | 5 |
| 109 | 1.478 | 1.479 |  | 4 |
| 208 | $1 \cdot 420$ | $\{1.422$ | 19 | 3 |
| 220 | 1420 | \{ 1.419 | 19 | 14 |

The significant interatomic distances are:

| $\mathrm{Ba}(1)-\mathrm{Ba}(2)$ | $3.913 \AA$ | $\mathrm{Ba}(2)-\mathrm{O}(1)$ | $2.824 \AA$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Ba}(1)-\mathrm{Fe}(1)$ | 3.479 | $\mathrm{Ba}(2)-\mathrm{O}(2)$ | 2.854 |
| $\mathrm{Ba}(1)-\mathrm{Fe}(2)$ | 3.539 | $\mathrm{Fe}(1)-\mathrm{Fe}(2)$ | 3.928 |
| $\mathrm{Ba}(1)-\mathrm{O}(1)$ | 2.850 | $\mathrm{Fe}(2)-\mathrm{O}(1)$ | 1.945 |
| $\mathrm{Ba}(2)-\mathrm{Fe}(1)$ | 3.549 | $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.880 |

The best final data for the observed and calculated intensities and interplanar spacings are reported in Table 2.

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# The Crystal Structure of $\mathbf{1 H , 3 H}$-Naphtho[1,8]thiopyrane 

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#### Abstract

Crystals of $1 H, 3 H$-naphtho [1,8]thiopyrane, $\mathrm{C}_{12} \mathrm{H}_{10} \mathrm{~S}$, are monoclinic $\left(P 2_{1} / c\right)$ with $a=15 \cdot 2305, b=9 \cdot 0518$, $c=14.6491 \AA$ and $\beta=108.37^{\circ}$. There are two molecules in the asymmetric unit. No individual bond lengths deviate by more than three standard deviations from the corresponding average values. The lengths of the differently located bonds in the aromatic system agree well with those reported earlier for the naphthalene nucleus. The hetero-atom is $0.94 \AA$ out of the plane of the rest of the molecule.


## Introduction

In connexion with studies on ring systems containing sulphur and selenium atoms Biezais-Zirnis \& Fredga (1971) prepared some compounds with the heteroatoms attached to a 1,8 -dimethylnaphthalene nucleus. The crystal structure of $1 \mathrm{H}, 4 \mathrm{H}$-naphtho[1,8]diselenepine was earlier determined at this research unit (Aleby, 1972). In this connexion it was also considered desirable to perform an X-ray analysis of $1 \mathrm{H}, 3 \mathrm{H}$-naphtho[1,8]thiopyrane (NTP, I).

(I)

## Experimental

Recrystallization of NTP from petroleum spirit gave colourless crystals with a rhombic shape. The

